

# Correlation Measures for Solute Transport Model Identification & Evaluation

Fred Sonnenwald<sup>1</sup>, Virginia Stovin<sup>1</sup>,  
and Ian Guymer<sup>2</sup>

1 The University of Sheffield

2 The University of Warwick



The  
University  
Of  
Sheffield.

THE UNIVERSITY OF  
WARWICK

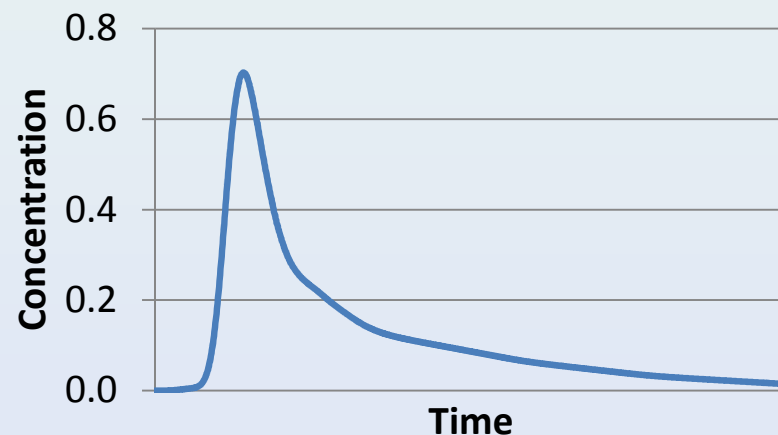
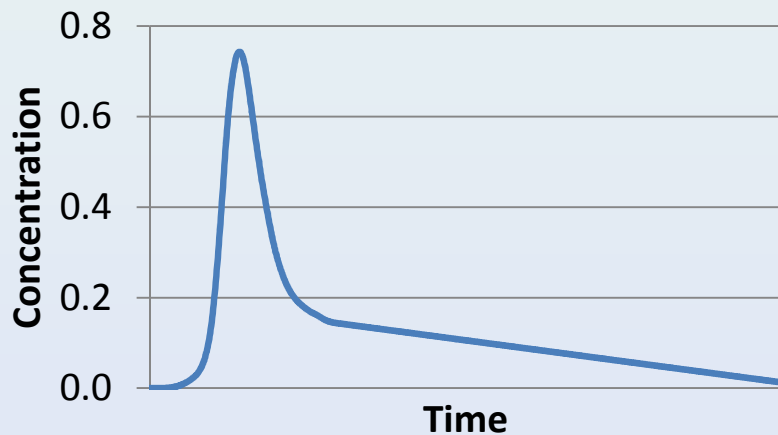
# Solute Transport Models

- Advection Dispersion Equations (ADE)
  - Aggregated Dead-Zone (ADZ)
  - Residence Time Distribution (RTD)
- 
- All take input, manipulate, produce output
  - *If the input is recorded data, there is usually recorded output to compare model output to*



# Correlation Measures

- Come in a variety of forms for a variety of purposes
- Describe the similarity between two time-series



# Identification & Evaluation

- In context they are two different, but related problems
- **Identification** is getting the model output to match the recorded data through adjustment of model parameters
- **Evaluation** is judging how well one model's output fits compared to another's or how well the model fits the recorded data

# Research Question

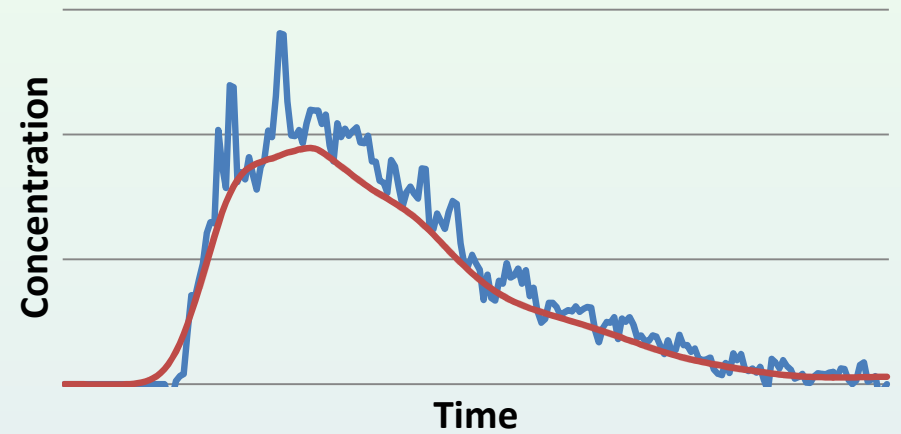
- Deconvolution is an optimisation process for finding the parameters that describe the residence time distribution (**Identification**)
- Multiple data sets lead to the generation of large numbers of parameterized models to be evaluated (**Evaluation**)
- Both use correlation measures - how do different correlation measures reflect the difference between measurement and model?



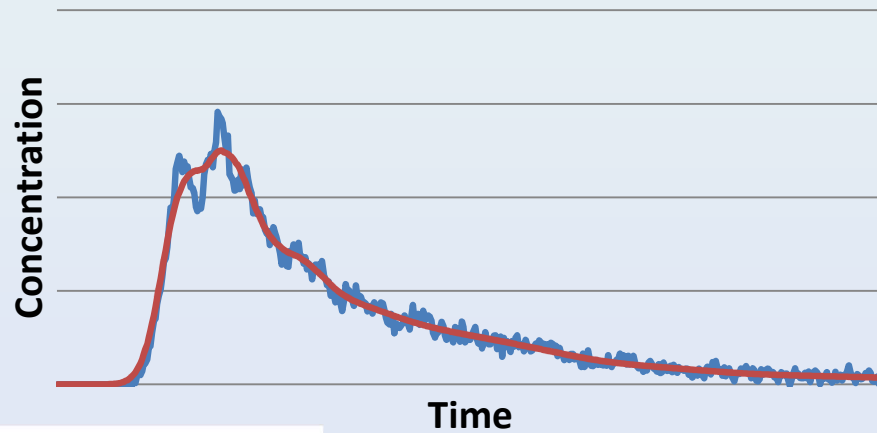
# Example ( $R_t^2$ )

- 0.96
- 0.99
- 0.999

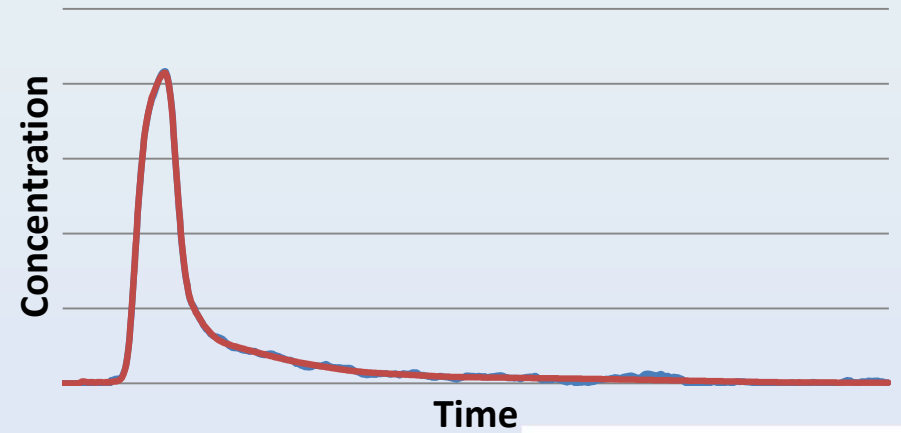
— Recorded — Model



— Recorded — Model



— Recorded — Model



The University  
Of  
Sheffield.

THE UNIVERSITY OF  
WARWICK

# Desirable Characteristics of Measures

- Sensitivity to Transformation (change in shape)
- Sensitivity to Transformation Magnitude (scale of change in shape)
- Insensitivity to noise
- Insensitivity to length of time-series (evaluation only)

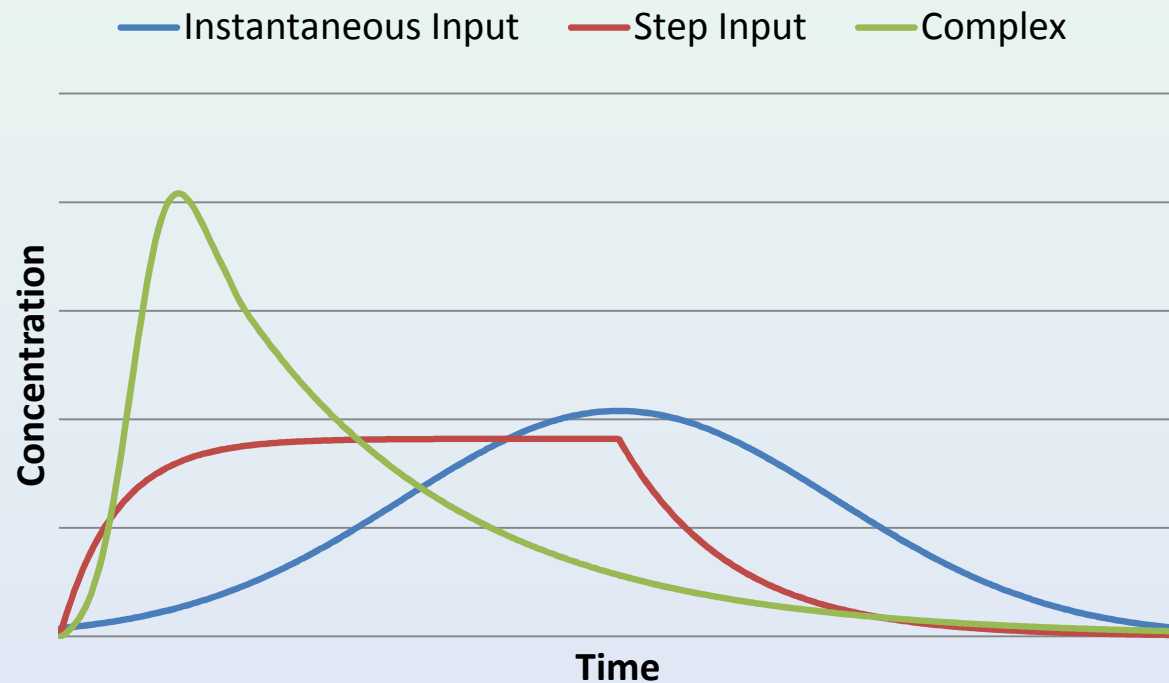
# Methodology

- Identified 12 correlation measures
  - BLC,  $\chi^2$ , FFCBS,  $R^2$ , PMCC, RMSD,  $R_t^2$ , SimilB, YIC, CORR2, ISE, APE
- Generated three test scenarios
- Applied transformations at different magnitudes, as well as noise
- Compared modified traces to unmodified traces
- Normalised results and compared



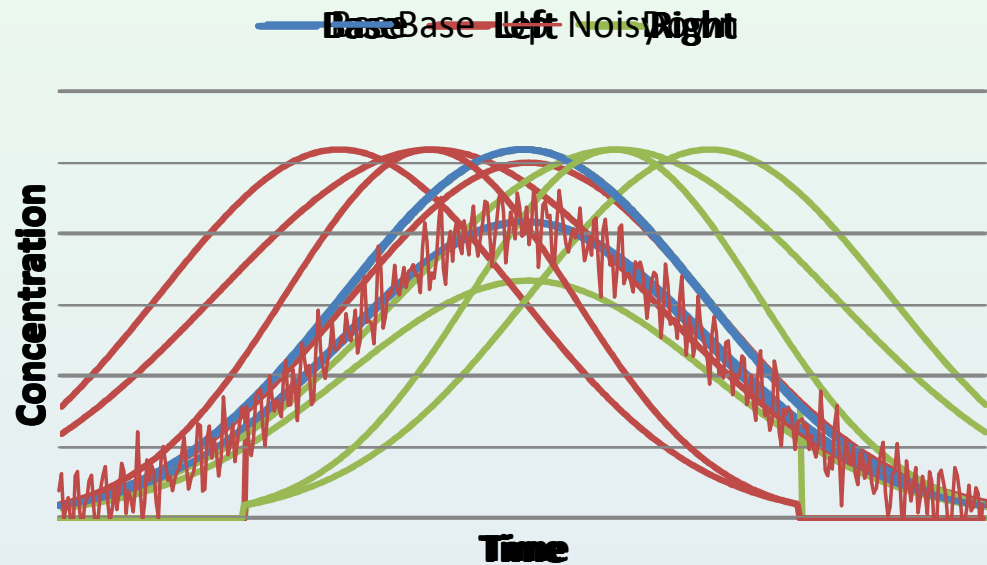
# Mixing Scenarios

- Instantaneous Input
- Step Input
- Complex



# Transformations

- Scaling
- Shifting
- Truncation
- Stretching
- Squeezing
  
- Noise

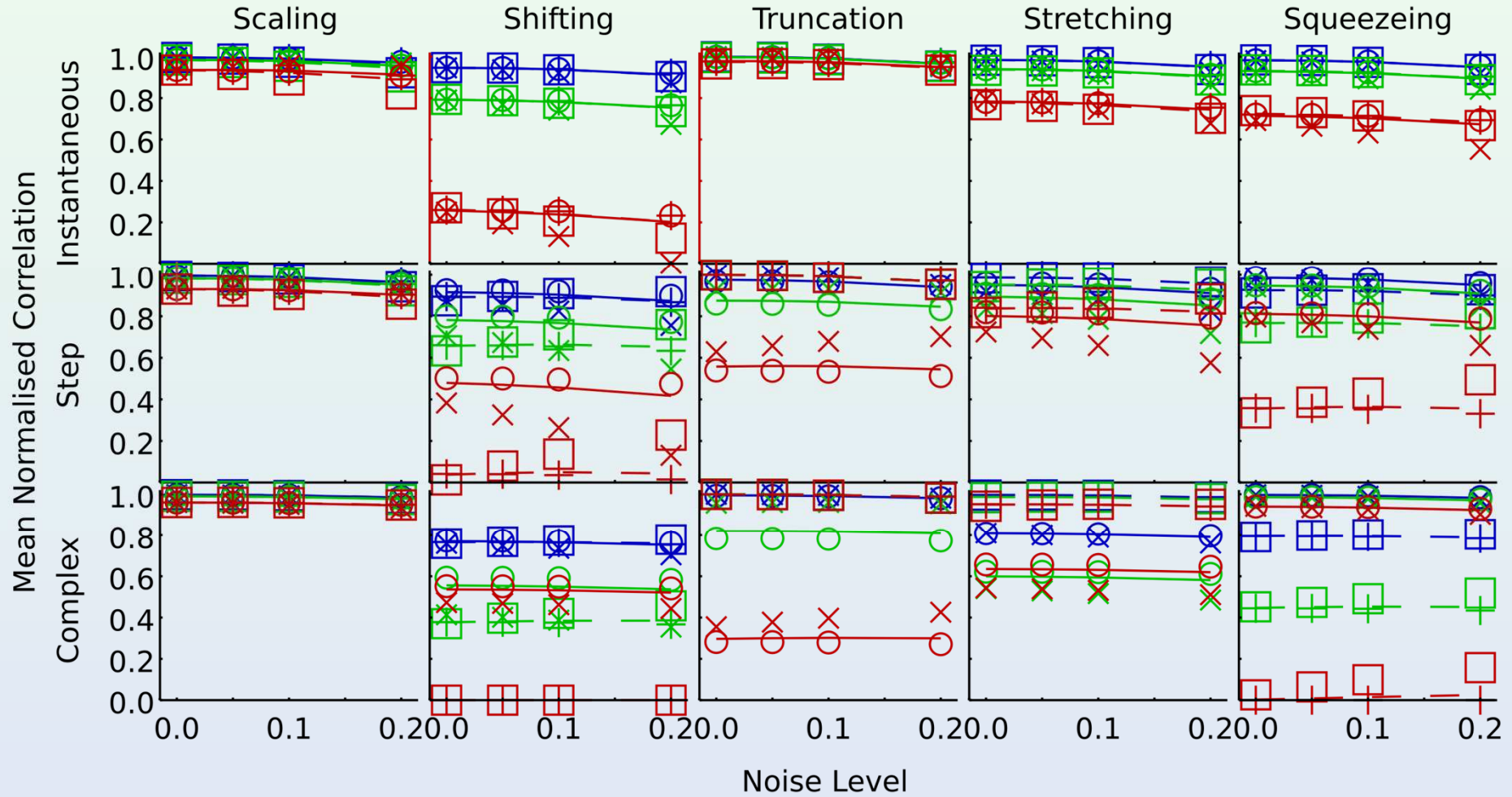


# Normalisation and Comparison

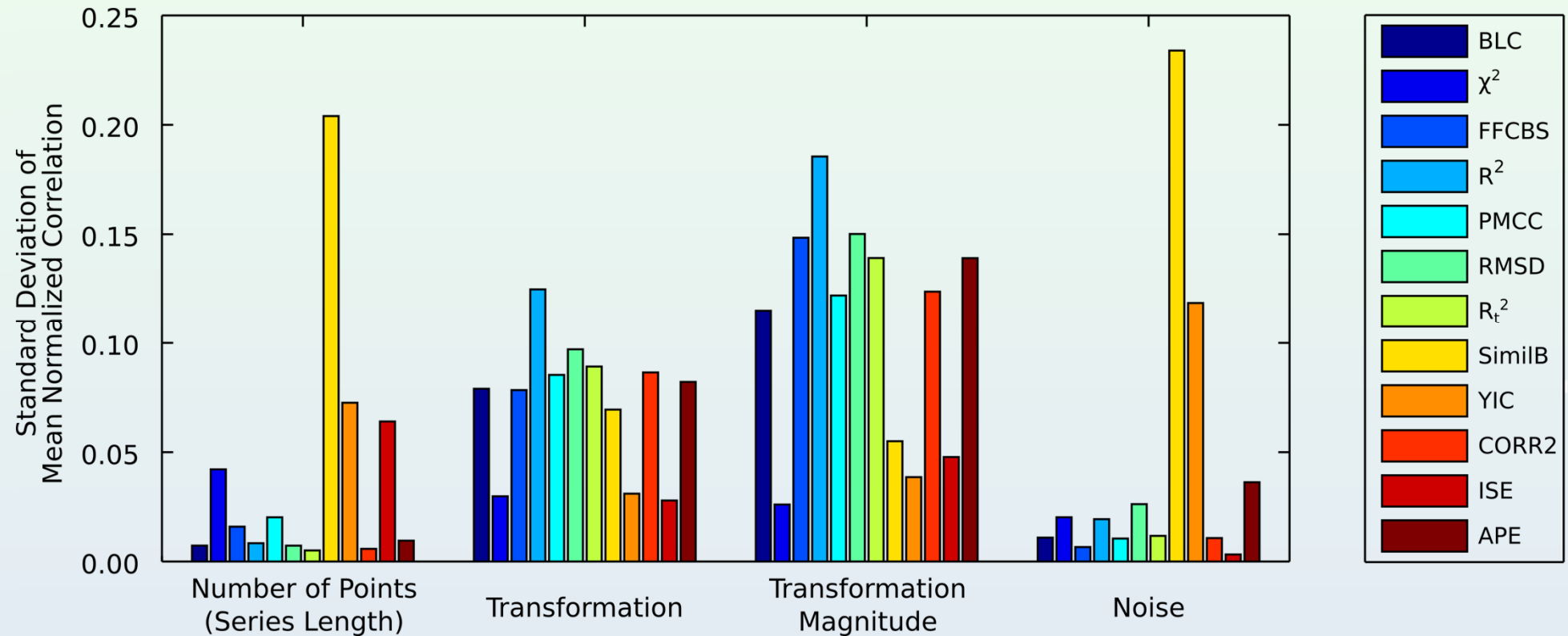
- Dimensional and non-dimensional correlation measures
- Possible to compare directly in plots
- *Standard deviation of correlation values with respect to each parameter indicates sensitivity to that parameter*



# Complete Plots



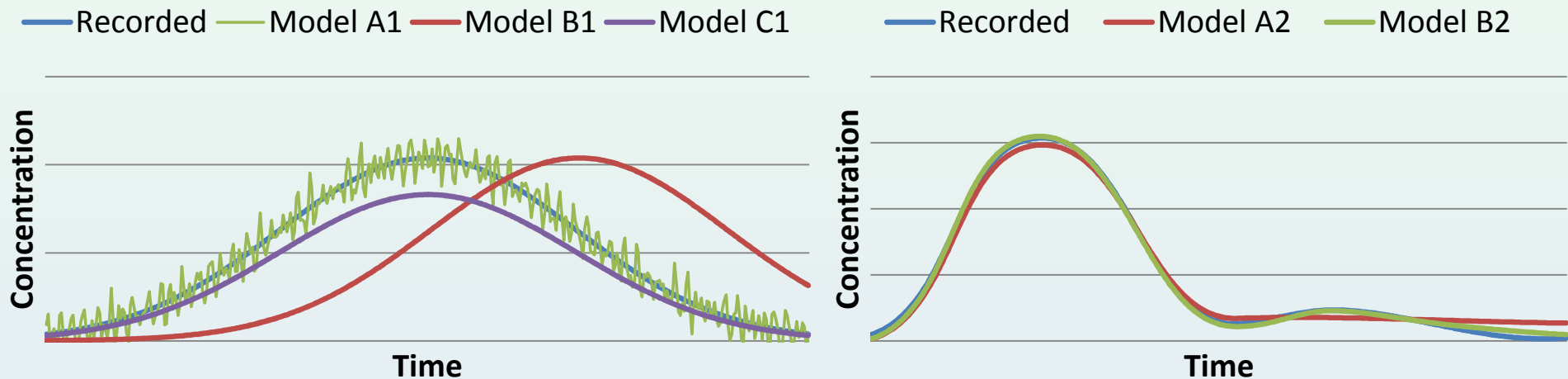
# Standard Deviation Plot



- BLC,  $\chi^2$ , FFCBS,  $R^2$ , RMSD,  $R_t^2$ , ISE, APE

# Application to Model Evaluation

- Non-dimensional measures ( $R^2$ ,  $R_t^2$ , APE)



- $R_t^2$  very elastic about indicating model fit
- $R^2$  very specific about defining overall shape
- APE reflects small differences extremely well

# Conclusion

- 8/12 measures found suitable for identification
  - BLC,  $\chi^2$ , FFCBS,  $R^2$ , RMSD,  $R_t^2$ , ISE, APE
- 3/8 measures found suitable for evaluation
  - $R^2$ ,  $R_t^2$ , APE
- *Different measures can be more suitable in different scenarios*



Thank you for listening



The  
University  
Of  
Sheffield.

THE UNIVERSITY OF  
WARWICK